Numerical Methods Practical Warks
$2^{\text {nd }}$ year of a bachelor's degree in computer science

## Practical Wark "02"

## V. Loups.

V.I While

A while loop executes a block of instructions as long as a logical expression is true.

## Syntax

```
while «expression>
    < Instructions >
end
```


## Example

In the script editor window, type:

| Commands |
| :---: |
| $\begin{aligned} & a=\square ; \\ & \text { while (a<3) } \\ & \quad \text { fprint ('The value of a: \%d } \% \text { n', a); } \\ & \quad a=a+1 \text {; } \\ & \text { end } \\ & \hline \end{aligned}$ |
| Results |
| The value of a: 0 The value of a : The value of a: 2 |

## V. 2 for

A for loop is used to repeat a block of instructions a given number of times.
Syntax

| for index $=$ value |
| :--- |
| <nnstructions> |
| end |

Value has one of the following forms:

| Form | Description |
| :---: | :---: |
| initVal :endVal | Increments the index variable from <br> initVal to endVal by I. |
| initVal $:$ step : <br> endVal | Index increments by step value in <br> each iteration, or decrements <br> when step value is negative. |
| Values from a a <br> vector | The index variable takes the values <br> af a given vector. |

## Example

In the script editor window, type:

| Commands |
| :---: |
| ```fora=10:15 fprint('The value of a: %d\n', a); end``` |
| Results |
| The value of a: 10 |
| The value of a: 11 |
| The value of a: 12 |
| The value of a: 13 |
| The value of a: 14 |
| The value of a: 15 |

## Example

In the script editor window, type:

| Commands |
| :--- |
| for a $=10: 2: 15$ <br> fprinf( ('The value of a: \%d $/ n$ ', a); <br> end |
| Results |
| The value of a: 10 <br> The value of a: 12 <br> The value of a: 14 |

## Example

In the script editor window, type:

| Commands |  |
| :--- | :--- |
| for $a=\left[\begin{array}{lll}1015 & 20\end{array}\right.$ <br> disp (a) |  |
| end |  |

## V. 3 Lopss cantral

## V.3.I The break instruction

The break instruction ends the execution of a far or while loap then transfers the execution to the instruction immediately following the loap.

## Example

In the script editor window, type:

| Commands |
| :---: |
| ```for i=1:10 if mod(i,2)==1 disp(i) else break disp(i+j) % j is the imaginary unit \sqrt{}{-1} end end``` |
| end Results |
| 1 |

## V.3.I The instruction continue

The continue instruction is used to pass control to the next iteration of for ar while i.e., continue skips the rest of the code in its body and immediately tests the condition before repeating.

## Example

In the script editor window, type:

| Commands |
| :---: |
| ```for i=1:1[] if mad(i,2)== 1 disp(i) else continues disp(i+j) % j is the imaginary unit \sqrt{}{-1}}\mathrm{ . end end``` |
| Results |
| 3 <br> 5 <br> 7 |

## VI. Vectars.

In the command window, type the expressions

| Cammands | Results |
| :--- | :--- |


| $\gg \mathrm{A}=[123510]$ | $A=123510$ |
| :---: | :---: |
| $\gg \mathrm{B}=[10,12,-5]$ | $B=1012-5$ |
| > $>$ [ $=[5 ; 0 ; 1]$ | $\begin{array}{r} C=5 \\ 0 \\ 1 \end{array}$ |
| $\gg \mathrm{D}=[10:-2: 1]$ | D=108542 |
| $\begin{aligned} & \gg E=[11: 12 ; 30 ; 41 ; 15] ; \\ & \gg E(3) \end{aligned}$ | years $=30$ |
| $\begin{aligned} & \gg F=\left[\begin{array}{ll} 1 & 3 \end{array}\right] ; \\ & \gg F(:) \end{aligned}$ | years $=123$ |
| $\begin{aligned} & \gg=[12345678] ; \\ & \gg \text { sub } G=G(3: G) \end{aligned}$ | sub_¢ $=3456$ |

## VI.I Vector creation

MATLAB lets you create two types of vectars: row vectors and column vectors.

## VI.I.I Line vectar

To create line vectors, simply apen a bracket, write the elements of the vector using a space or comma to separate them, then clase the bracket as follows: $\left[x_{1}, x_{2}, x_{3}, \ldots, x_{n}\right]$ वг $\left[\begin{array}{lllll}x_{1} & x_{2} & x_{3} & \ldots & x_{n}\end{array}\right]$.

## VII.I. Column vectar

Column vectors are created in the same way as row vectors but using a semicolon to separate the elements as follows:
$\left[x_{1} ; x_{2} ; x_{3} ; \ldots ; x_{n}\right]$.

## VI. 2 Elements access

You can refer to one ar mare elements of a vector in different ways, where the $i^{i^{\prime} e m e}$ component of a vector $v$ is called $v(i)$.

1. To access a single element, simply write vector_name(element_index).

| Cammands | Results |
| :--- | :--- |
| $\gg$ vect $=[103107 \mathrm{Q}\\| \\| 3-10] ;$ |  |
| $\gg$ vect $(5)$ | ans $=\\| \\| 3$ |

2. To access a finite set of vector elements, simply write vector_name (firstElement|ndex : lastElementIndex).

Example

| Cammands | Results |
| :--- | :---: |
| $\gg$ vect $=[10: 50] ;$ |  |
| $\gg$ vect $(20: 25)$ | ans $=293031323334$ |

3. To access all the elements of a vector, simply write vector_name (:)

Example

| Commands |  | Results |
| :--- | :--- | :--- |
| $\gg$ vect $=[1: 0.2: 2] ;$ |  |  |
| $\gg$ vect (:) | ans $=1$ | 1.2 |

## VI. 3 Elements madification

Vector elements can be modified by assigning new values to them.

Example

| Commands | Results |
| :--- | :---: |
| $\gg v=[12345] ;$ |  |
| $\gg v(5)=v(3)-v(2) ;$ |  |
| $\gg$ disp $(v)$ | $v=12341$ |

MATLAB also has a table editor that lets you modify the dimensions and entries of a vector ar matrix. To use this editar, double-click on the variable to be edited in the Workspace.

## VI. 4 Vector aperations.

VI.4.I Addition and subtraction.

You can add or subtract two vectars. Both vectars must be of the same type and have the same number of elements.

## Example

In the script editar window, type:

| Commands |
| :--- |
| $A=[7, I I, I 5,23, ~ I] ;$ |
| $B=[2,5, I 3, I B, 20] ;$ |
| $C=A+B$ |
| $D=A-B$ |

VI.4.2 Multiplication by a scalar.

Multiplying a vector by a number praduces a new vector of the same type, with each element of the original vector multiplied by the chosen number.

## Example

In the command window, type:

| Cammands | Results |
| :---: | :---: |
| $\gg$ vect $=[12$ 34 ID 8]; |  |
| $\gg$ newVect $=5^{*}$ vect | newVect $=$ 60 17050 40 |

## VI.4.3 Transposed vector.

The transposition operation changes a column vector into a row vector and vice versa. The transposition operation is represented by $\left.{ }^{( }\right)$.

## Example

In the command window, type:

| Commands | Results |
| :--- | :---: |
| $\gg$ vect $=[1234$ ID 8$]$ | vect $=1234108$ |
| $\gg$ transVect $=$ vect' | transVect $=12$ |
|  | 34 |
|  | 10 |
|  | 8 |

## VI.4.4 The scalar praduct (lnner product).

 In MATLAB, you can calculate the scalar product of two vectors using the dot command.
## Example

In the command window, type:

| Commands | Results |
| :--- | :--- |
| $\gg$ vect $=[5673] ;$ |  |
| $\gg$ vect2 $=[1234] ;$ |  |
| $\gg$ vect3 $=$ dat (vectl, vect2) | vect3 $=74$ |

Both vectars must have the same number of elements. In mathematics, the inner product of $A=\left[\begin{array}{llll}x_{1} & x_{2} & \ldots & x_{n}\end{array}\right]$ and $A=\left[\begin{array}{llll}y_{1} & y_{2} & \ldots & y_{n}\end{array}\right]$ is:

$$
\text { A. } B=\sum_{i=1}^{n} x_{i} \times y_{i}
$$

## VI.4. 5 Vectars' concatenation.

MATLAB lets you add vectors tagether to create new vectors.

1) The concatenation of two line vectors In the command window, type:

| Commands | Results |
| :--- | :---: |
| $\gg$ vect $=[1082] ;$ |  |
| $\gg$ vect2 $=[0035] ;$ |  |
| $\gg$ vect3 $=[$ vect 1 vect2] $]$ | vect3 $=10820035$ |
| $\gg$ vect4 $=[$ vectl; vect2 $]$ | vect4 $=1082$ |
|  | 0035 |

To perform the secand concatenation, bath vectors must have the same number of elements.
2) The concatenation of two column vectars In the command window, type:

| Commands | Results |
| :--- | :---: |
| $\gg$ vect $=[0 ; 1 ; 2] ;$ |  |
| $\gg$ vect $2=[3 ; 5] ;$ |  |
| $\gg$ vect $3=[$ vectl; vect2 $]$ | vect3 $=0$ |
|  | 1 |
|  | 2 |
|  | 3 |
|  | 5 |
| $\gg$ vect $4=[I[; 20] ;$ |  |
| $\gg$ vect $5=[$ vect2 vect4 $]$ | vect $4=310$ |
|  | 520 |

To perform the second concatenation, both vectors must have the same number of elements.

## VI.4.B Dther Dperations.

| Прегаtion | Description |
| :---: | :---: |
| .* | Multiply two vectors component by component. |
| ./ | Divide the components of two vectors in pairs. |
| $\wedge$ | Raise the components of one vector to the power of the components of the second vector. |
| sum(u) | Sum of the components of a vector. |
| mean(u) | Average of the components of a vector. |
| length(u) | Gives the length of a vector. |
| $\min (u)$ | Gives the smallest component of a vector. |
| $\max (u)$ | Gives the largest component of a vector. |

## VII. Matrices.

## VII.I Creating a matrix.

In MATLAB, you can create a matrix by entering elements in each row and using semicolons to mark the end of each row.

## Example

In the command window, type:

| Commands | Results |
| :---: | :---: |
| $\begin{aligned} & \text { >>MI = [12345;2345 } \\ & \text { 6;34567:45678] } \end{aligned}$ | $\begin{aligned} & M I= 12345 \\ & 23456 \\ & 34567 \\ & 45678 \end{aligned}$ |
| $\gg M 2=[1,2,3,4,5 ; 2,3$, 4, 5, 6: 3, 4, 5, 6, 7: 4, 5, 6, 7.8] | $\begin{aligned} & M 2= 12345 \\ & 23456 \\ & 34567 \\ & 45678 \end{aligned}$ |

VII. 2 Elements access.

1. To access an element in the $i^{i^{\prime} e m e}$ row and $i^{i}{ }^{\prime}$ eme column, we write matrix_name (row_index, column_index)

## Example

| Commands | Results |
| :---: | :---: |
|  |  |
| >> M (2, 3) | ans $=2$ |

2. To access all elements of a column matrix_name (: , column_index)

Example

| Commands | Results |
| :--- | :---: |
| $\gg M=[153: 492: 108] ;$ |  |
| $>M(: 3)$ | ans $=3$ |
|  | 2 |
|  | 9 |

3. To access all the elements of a line matrix_name (line_index, :)

Example

| Commands | Results |
| :--- | :---: |
| $\gg M=[153: 492: 108] ;$ |  |
| $\gg(1,:)$ | ans $=153$ |

4. You can access all the elements of several lines by matrix_name (indexFirstLine : lastLinelndex, :)

Example

| Commands | Results |
| :--- | :---: |
| $\gg M=[153: 492: 108] ;$ |  |
| $>M(2: 3,:)$ | ans $=492$ |
|  | 109 |

5. You can access all the elements of several columns by matrix_name (: firstaolumnindex : last[alumnlndex)

Example

| Commands | Results |
| :---: | :---: |
| $\gg \mathrm{M}=[153 ; 4$ 2 2110 l ]; |  |
| >> M (:, 2: -1:1) | $\begin{array}{r} \text { ans }=51 \\ 94 \\ 01 \end{array}$ |

6. You can access a sub-matrix matrix_name (firstRowlndex : lastRowIndex, firstLolumnlndex : last[olumnlindex)

Example

| Commands | Results |
| :---: | :---: |
|  |  |
| >> $\mathrm{M}(2: 3,2: 1-1: 1)$ | $\begin{array}{r} \text { ans }=94 \\ 01 \end{array}$ |

## VII. 3 Elements Madification.

You can modify the elements of a matrix by selecting the elements to be modified and assigning them new values

## Example

| Cammands | Results |
| :---: | :---: |
| $\gg M=[1234 ; 5678] ;$ |  |
| $>M(1: 2,2: 3)=[12 ; 33]$ | ans $=1124$ |
|  | 5538 |
|  |  |

MATLAB also has a table editor that lets you modify the dimensions and entries of a vectar ar matrix. To use this editar, double-click on the variable to be edited in the Workspace.
VII. 4 Deleting raws ar columns.

You can delete a row or column from a matrix by assigning an empty set of brackets [] to that row or column. [] denotes an empty matrix.

## Example

In the command window, type

| Commands | Results |
| :--- | ---: |
| $\gg M=[12345 ; 2345$ |  |
| $6 ; 34567 ; 45678] ;$ |  |
| $\gg M(4,:)=[]$ | $M=12345$ |
|  | 23456 |
|  | 34567 |
| $>L=M ;$ |  |
|  |  |
| $>L(:, 2)=[]$ | 2435 |
|  | 356 |
|  | 3567 |

## VII. 5 Dperation on matrices.

## VII.5.I Addition and subtraction.

You can add or subtract two matrices.
Both matrices must have the same number of rows and columns.

## Example

In the command window, type

| Commands | Results |
| :--- | :---: |
| $\gg A=[123 ; 456 ; 789] ;$ |  |
| $>B=[987 ; 654 ; 321] ;$ |  |
| $\gg=A+B$ | $C=1010$ |
|  | 101010 |
|  | 101010 |
| $>D=A-B$ | $0=-8-B-4$ |
|  | -202 |
|  | 468 |

## VII.5. 2 Scalar operations.

When you add, subtract, multiply or divide a matrix by a number, this is called a scalar operation.
Scalar operations produce a new matrix with the same number of rows and columns, with each element of the original matrix added, subtracted, multiplied by or divided by the number.

## Example

In the command window, type

| Commands | Results |
| :--- | :---: |
| $\gg \mathrm{M}=[101224 ; 148 \mathrm{~B} ; 288 \mathrm{ID}] ;$ |  |
| $\gg \mathrm{s}=2 ;$ |  |
|  |  |
| $\gg \mathrm{A}=\mathrm{M}+\mathrm{s}$ | $\mathrm{A}=121426$ |
|  | 16108 |
|  | 301012 |
| $>\mathrm{S}=\mathrm{M}-\mathrm{s}$ | $\mathrm{S}=81022$ |
|  | 1264 |
|  | 2668 |
| $\gg \mathrm{P}=\mathrm{M}^{*} \mathrm{~s}$ | $\mathrm{P}=202448$ |
|  | 281612 |
|  | 561620 |
| $>\mathrm{D}=\mathrm{M} / \mathrm{s}$ | $\mathrm{D}=5612$ |
|  | 743 |
|  | 1445 |

## VII.5. 3 Matrix division.

You can divide two matrices using left ( $\backslash$ ) or right (/) division operators. Both matrices must have the same number of rows and columns.

## Example

In the script editor, type


|  |
| :---: |
|  |  |
|  |  |
|  |  |
|  |  |

Note
I. $A / B$ is the solution to the equation $x B=A$.
2. $A \backslash B$ is the solution to the equation $A x=B$.

## VII. 5.4 Transposed matrix.

The transposition operation switches rows and columns in a matrix. It is represented by a single quatient (').

## Example

In the command window, type

| Commands | Results |
| :---: | :---: |
| $\gg \mathrm{A}=[101223 ; 148 \mathrm{~B} ; 278 \mathrm{~B}]$ | $\mathrm{A}=121223$ |
|  | 1486 |
|  | 2789 |
| $>\mathrm{B}=\mathrm{A}^{\prime}$ | $\mathrm{B}=101427$ |
|  | 1288 |
|  | 2369 |

## VII. 5.5 Concatenation of matrices.

MATLAB lets you concatenate matrices in two ways:

## l) Harizontal concatenation

In the script editor, type

|  |
| :---: |
|  |
|  |  |
|  |
| $A=101223123145$ |
| 148680-9 |
| 278945211 |

2) Vertical concatenation

In the script editar, type

| Commands |
| :---: |
|  |
| Results |
| $B=101223$ |
| 1485 |
| 2789 |
| 123145 |
| 80-8 |
| 45211 |

## VII.5.6 Multiplication of matrices.

In the command windaw, type

| Commands | Results |
| :--- | :---: |
| $\gg \mathrm{M}=[123 ; 234 ; 125] ;$ |  |
| $>\mathrm{N}=[213 ; 50-2 ; 23-1] ;$ |  |
| $\gg \mathrm{P}=\mathrm{M}^{*} \mathrm{~N}$ | $\mathrm{P}=1810-4$ |
|  | $2714-4$ |
|  | $2216-6$ |

## VII.5. 7 Determinant.

The determinant of a matrix is calculated using MATLAB's det function.

## Example

In the command window, type

| Commands | Results |
| :--- | :--- |
| $\gg=[123 ; 234 ; 125] ;$ |  |
| $\gg \operatorname{det}(A)$ | ans $=-2$ |

VII. 5.8 Inverse of a matrix.

The inverse of a matrix is calculated using MATLAB's inv function.

Example
In the command windaw, type

| Commands | Results |
| :--- | :---: |
| $\gg \mathrm{A}=[123 ; 234 ; 125] ;$ |  |
| $\gg$ inv(A) | ans $=-3.520 .5$ |


|  | $3-1-1$ |
| :---: | :---: |
|  | -0.500 .5 |

## VII. B Special matrices

In the command window, type

| Commands | Results |
| :---: | :---: |
| >> zeros (3) | $\begin{array}{r} \hline \text { ans }=000 \\ 000 \\ 000 \end{array}$ |
| >> zeros (3,2) | $\begin{array}{r} \hline \text { ans }=00 \\ 00 \\ 00 \\ \hline \end{array}$ |
| >> ones (4,3) | $\begin{array}{rr} \hline \text { ans }= & 111 \\ 111 \\ 111 \\ 111 \\ \hline \end{array}$ |
| >> eye (4) | $\begin{array}{r} \text { ans }=1000 \\ 0100 \\ 0.10 \\ 0001 \end{array}$ |
| >> eye ( 3,4 ) | $\begin{array}{r} \text { ans }=1000 \\ 0100 \\ 0010 \\ \hline \end{array}$ |

## Remarks

| Contral | Description |
| :---: | :---: |
| zeros () | The zeras () function creates a null <br> matrix. |
| ones () | The anes () function creates a <br> matrix of I's. |
| eye () | The eye () function creates an <br> identity matrix. |

## VIII. Functians.

A function is a group of instructions that together perform a task (similar to scripts but scripts don't have parameters or inputs.). In MATLAB, functions are defined in separate files. The name of the file and the function must be the same.

## Syntax

function [out, out2, ..., out ${ }_{n}$ ] = myfun (in, in2, ..., in ) instructions
end

Here, the name of the function is myfun, inı to inn are the inputs or the parameters and outito outn are the outputs ar the results of the execution of the function.

## Example

In the script editar window, type this code and
save it as mymax

```
function max \(=\) mymax (nl, n2, n3, n4, n5)
    \(\max =\mathrm{nl}\);
    if (n2 > max)
        \(\max =n 2 ;\)
    end
    if ( \(\mathrm{n} 3>\max\) )
        \(\max =n 3 ;\)
    end
    if (n4 > max)
        \(\max =n 4 ;\)
    end
    if ( \(\mathrm{n} 5>\max\) )
        \(\max =n 5 ;\)
        end
end
```

In the command window, type

| Cammands | Results |
| :---: | :---: |
| $\gg$ mymax $(5,7,19,0,23)$ | ans $=23$ |

## Note

Function files aгe program files with .m extension.

